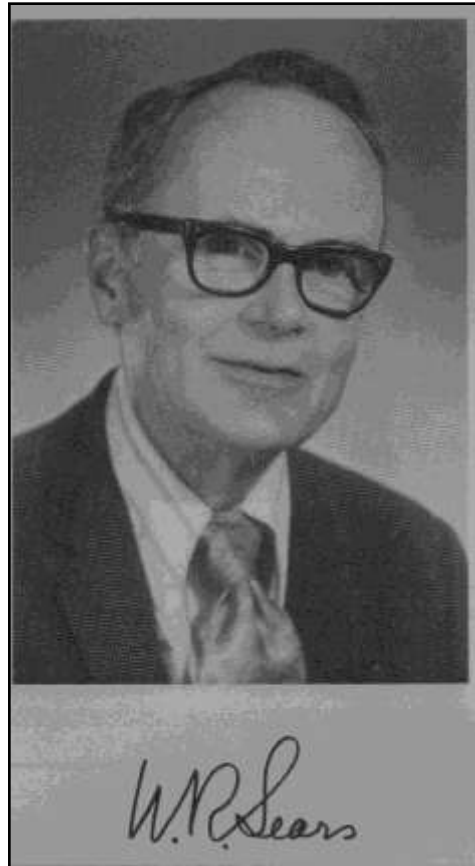


IN MEMORIAL TO THE LATE WILLIAM R. SEARS  
1913 – 2003



**“The Case of the Unsteady Boundary Layer Separation”**

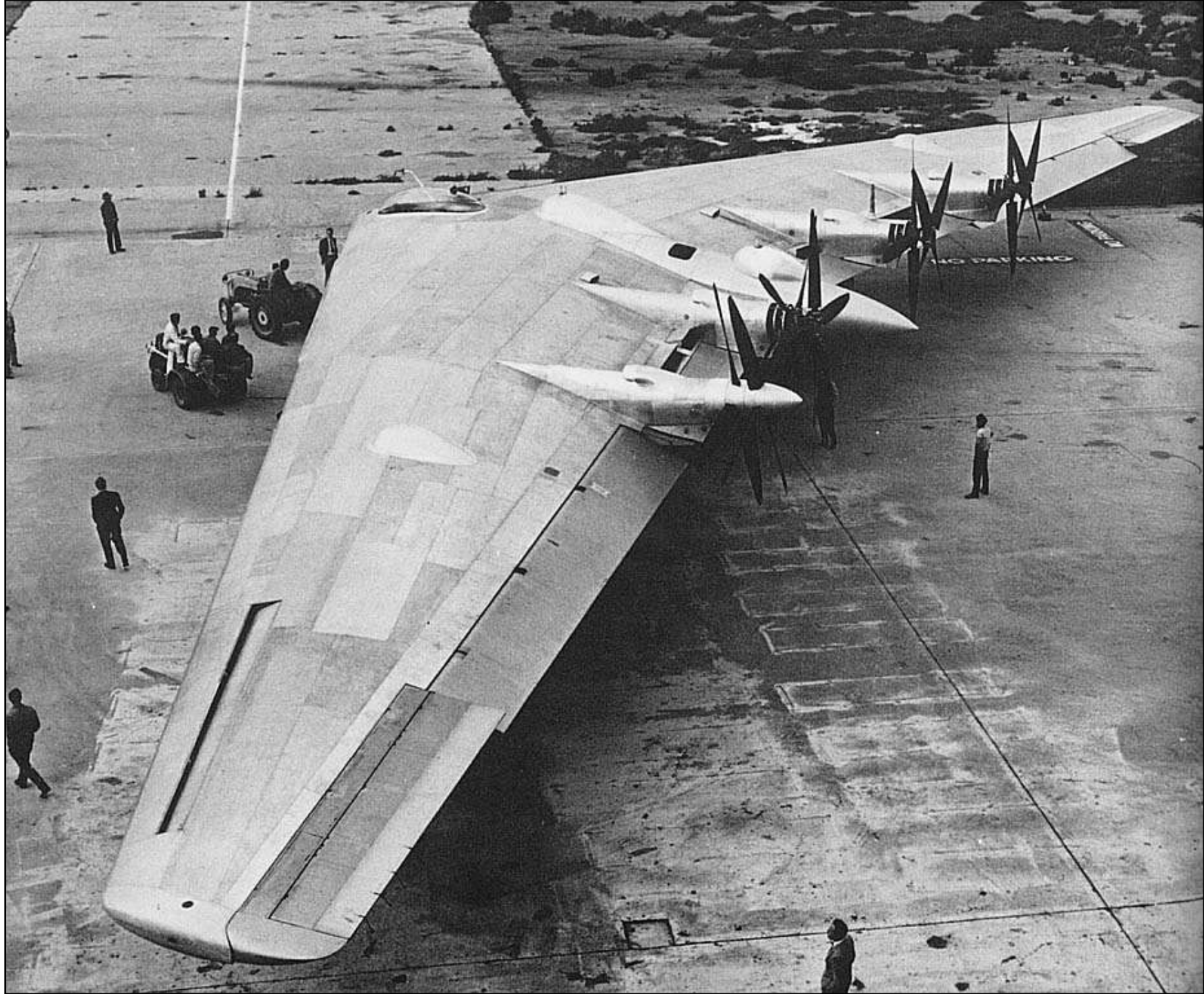
- 1938 PhD from Caltech with Theodore von Karman (Ludwig Prandtl)
- 1940 Assistant Professor at Caltech
- 1941 Joined Northrop Aircraft Company as Chief of Aerodynamics and Flight Testing (age 28)
  - P61 Black Widow
  - Flying Wing
    - [XB35](#)
    - YB49 → B2





**Northrop P-61C 'Black Widow'  
USAF Museum**



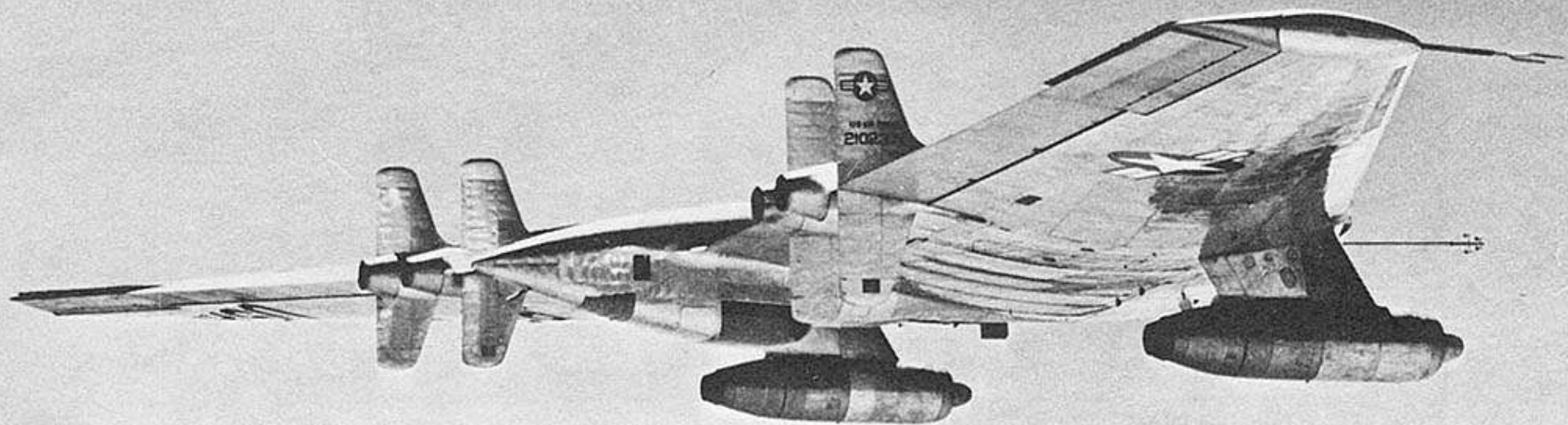






*this is a rare photo of nine Northrop Flying Wing Bombers.  
Many people do not realize that more than one or two prototypes were built of this design.  
Here, for the first time, is actual proof of their existence.  
Two of the big wing bombers are undergoing modifications from XB-35's to Flying Wing B-49 1t Bombers.  
The entire project was later cancelled by the Air Force.*





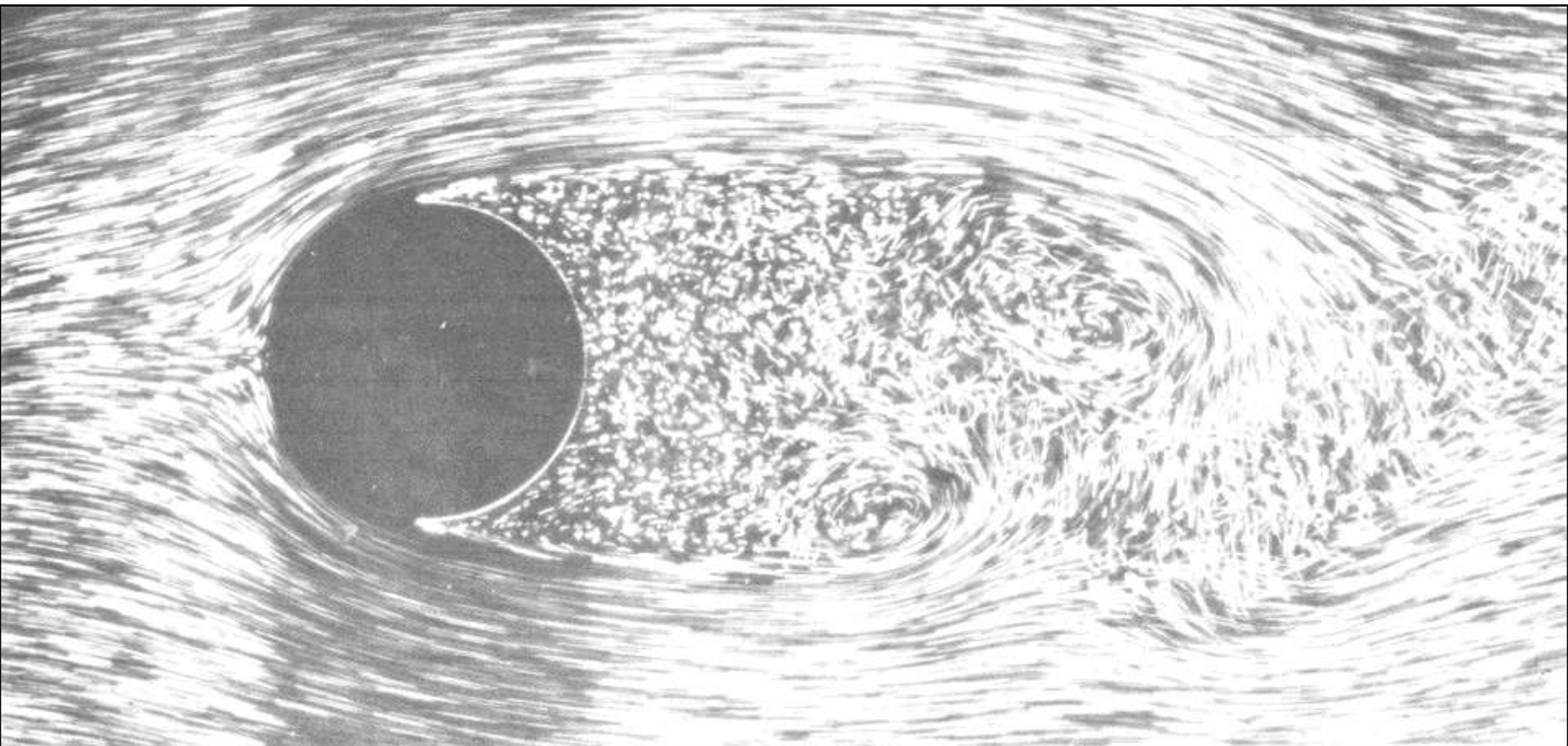
**Northrop-Grumman B-2 Spirit "stealth bomber."**

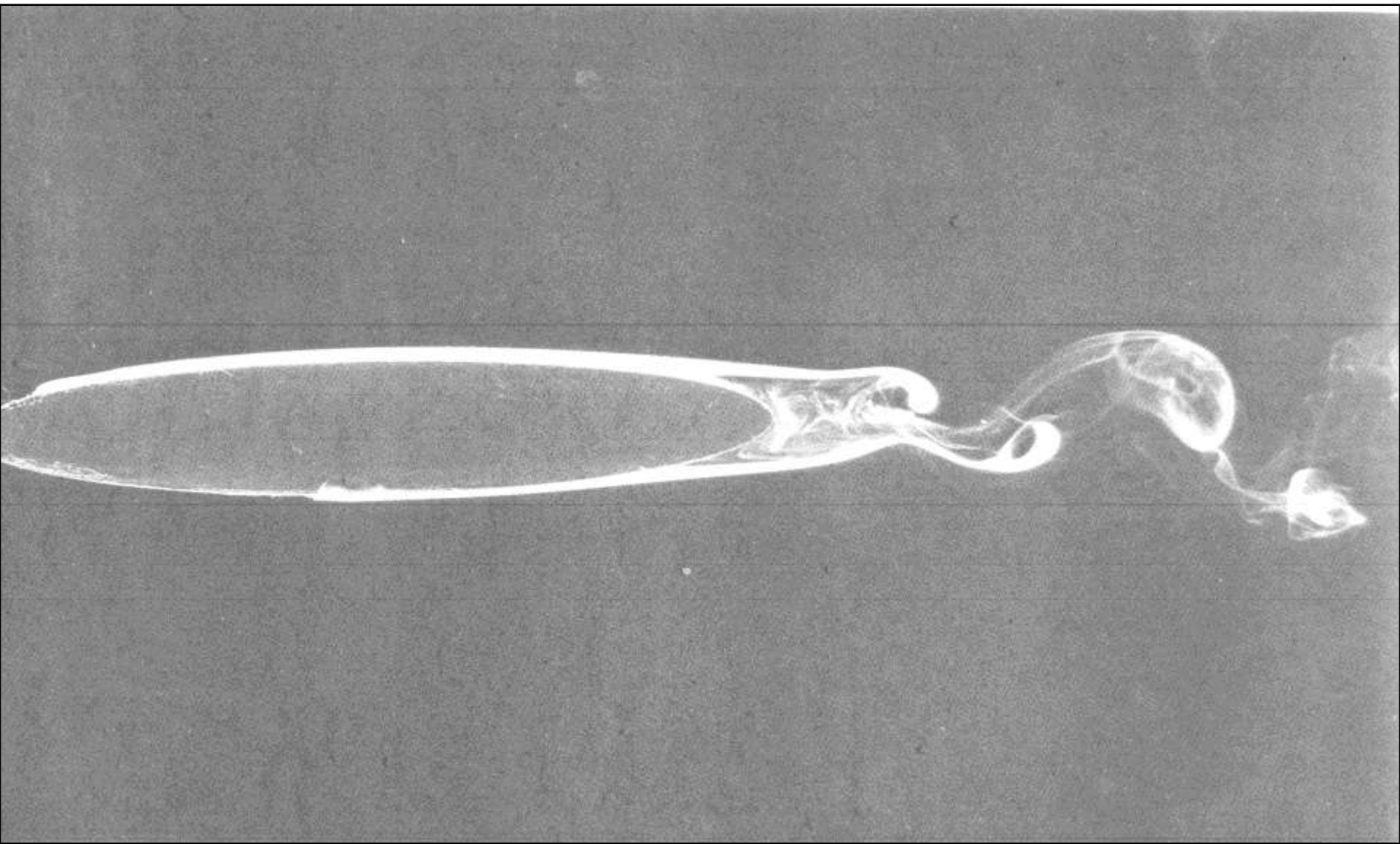


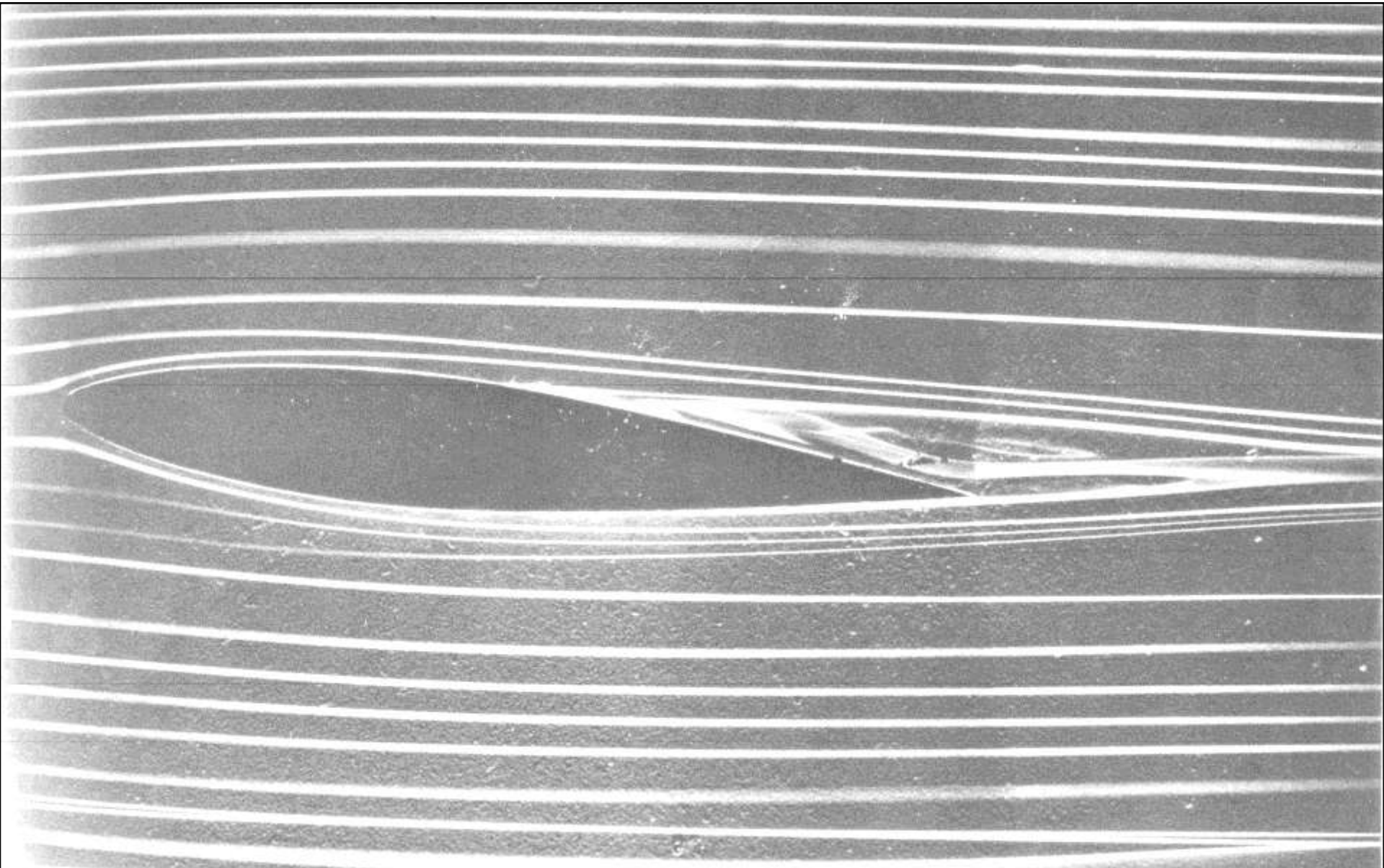
- 1947 Joined Cornell University, Director of the new Aero Graduate School

## Themes of Research

- 3-D Boundary Layers
  - Wing Theory
  - Unsteady Flow in Turbomachinery
  - Aerodynamic Noise
  - **Unsteady Boundary Layers and their Separation**
- 
- 1975 – 2003 Tuscon Arizona
  - (Univ. of Arizona, Aerospace and Mechanical Eng)



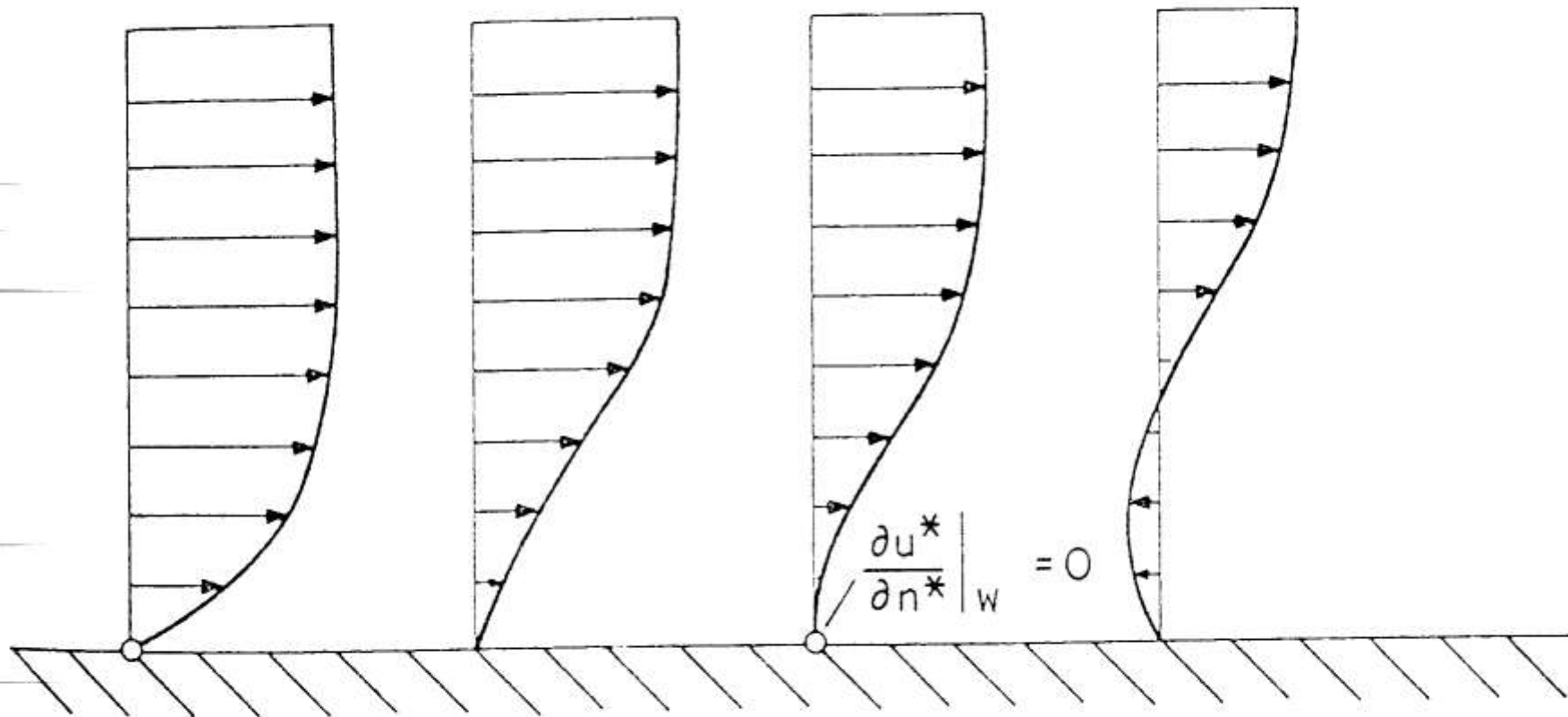




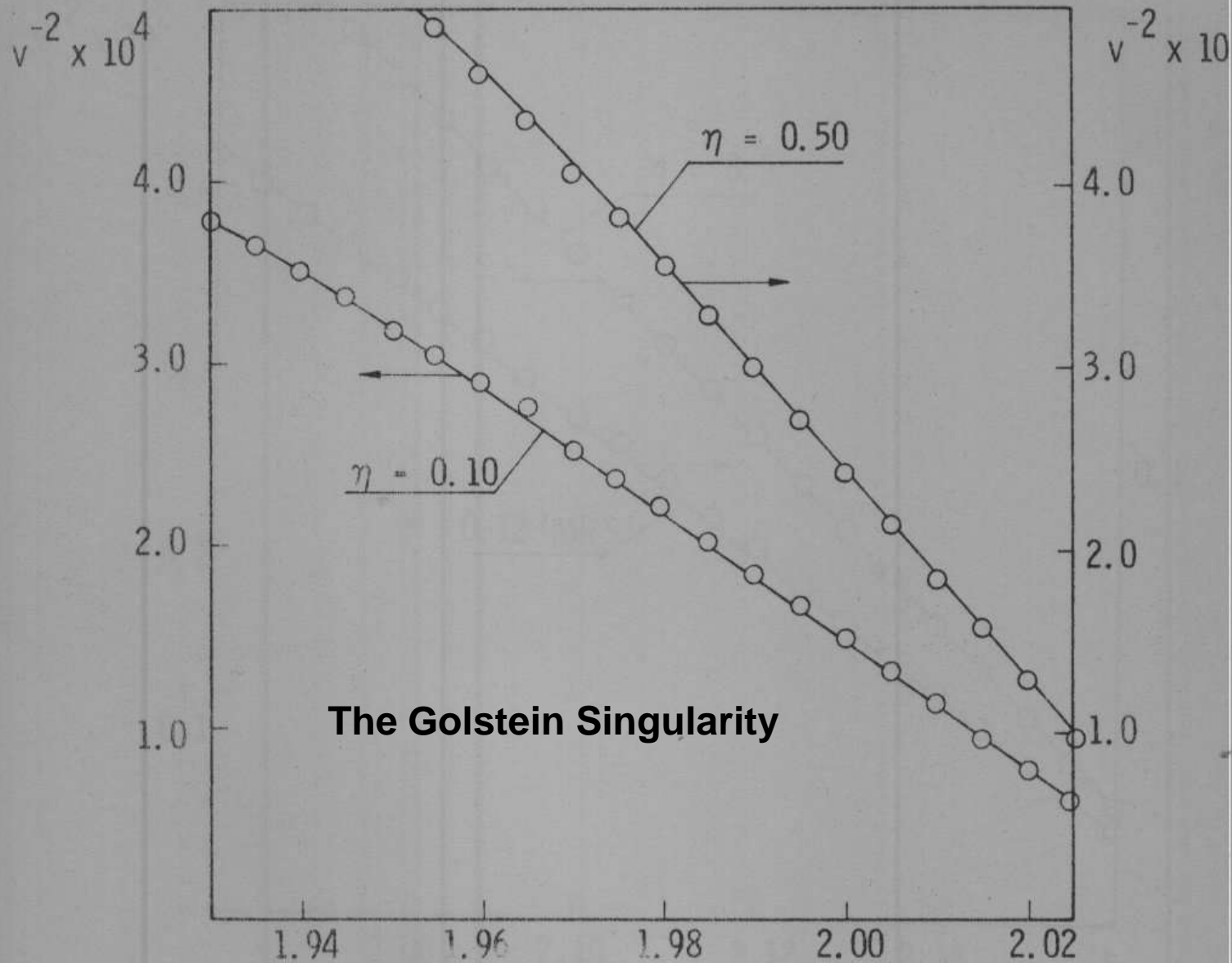
## Steady Boundary Layer Equations

$$\frac{\partial u}{\partial s} + \frac{\partial v}{\partial N} = 0$$

$$u \frac{\partial u}{\partial s} + v \frac{\partial u}{\partial N} = U_e \frac{dU_e}{ds} + \frac{\partial^2 u}{\partial N^2}$$

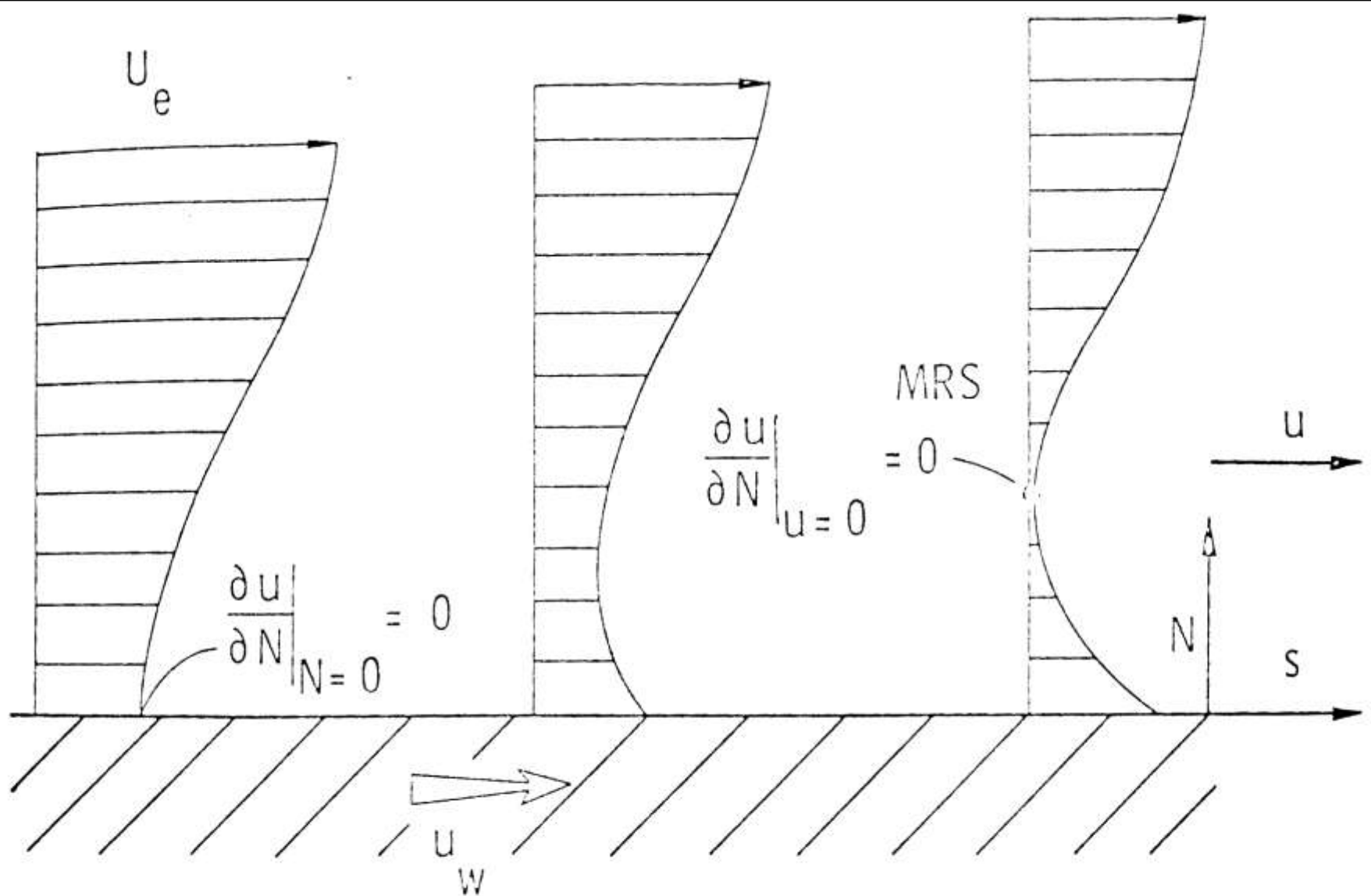


Schematic of the flow field in the neighborhood of a separation point.



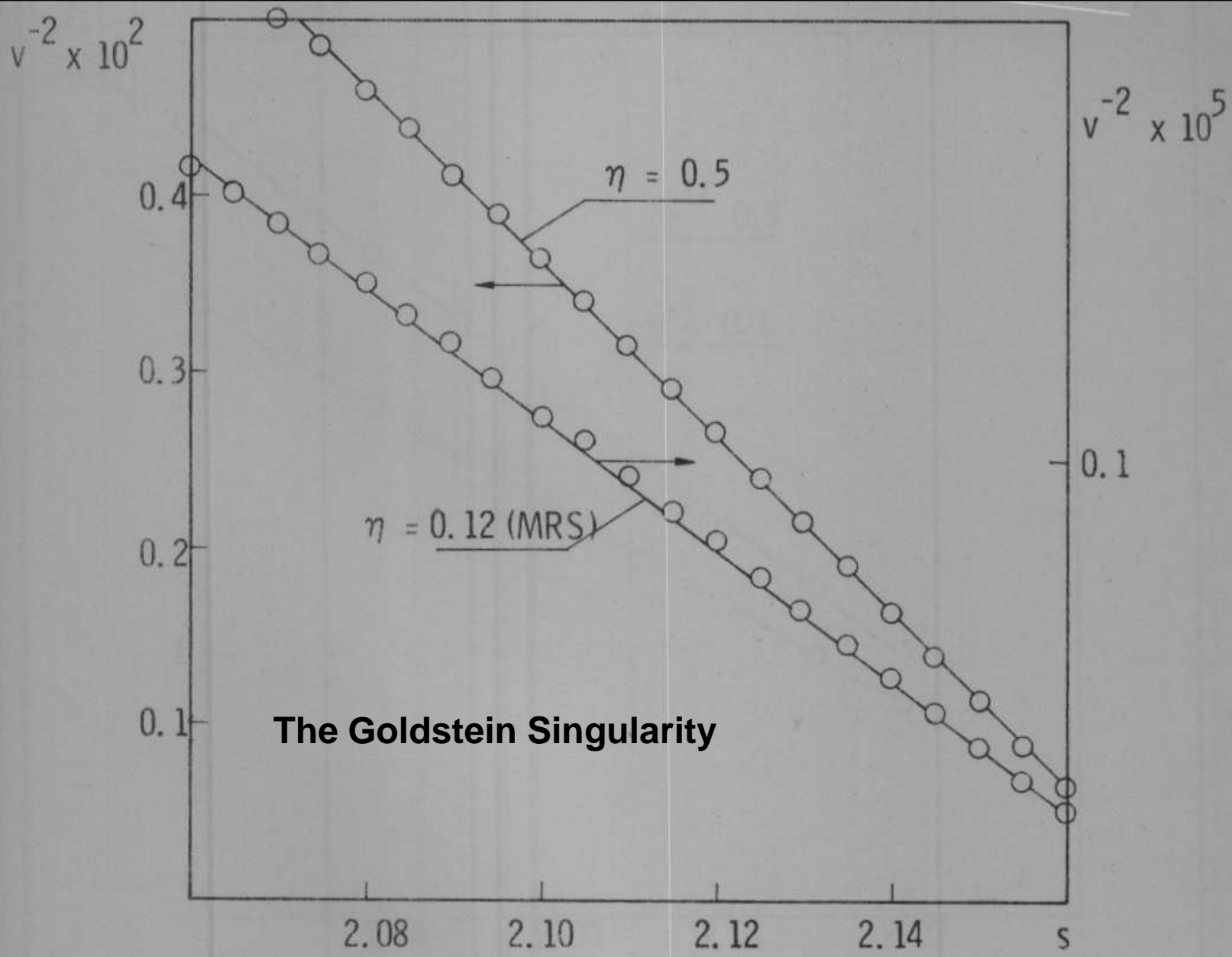
### The Golstein Singularity

The inverse square of the v-component versus s for stationary walls.



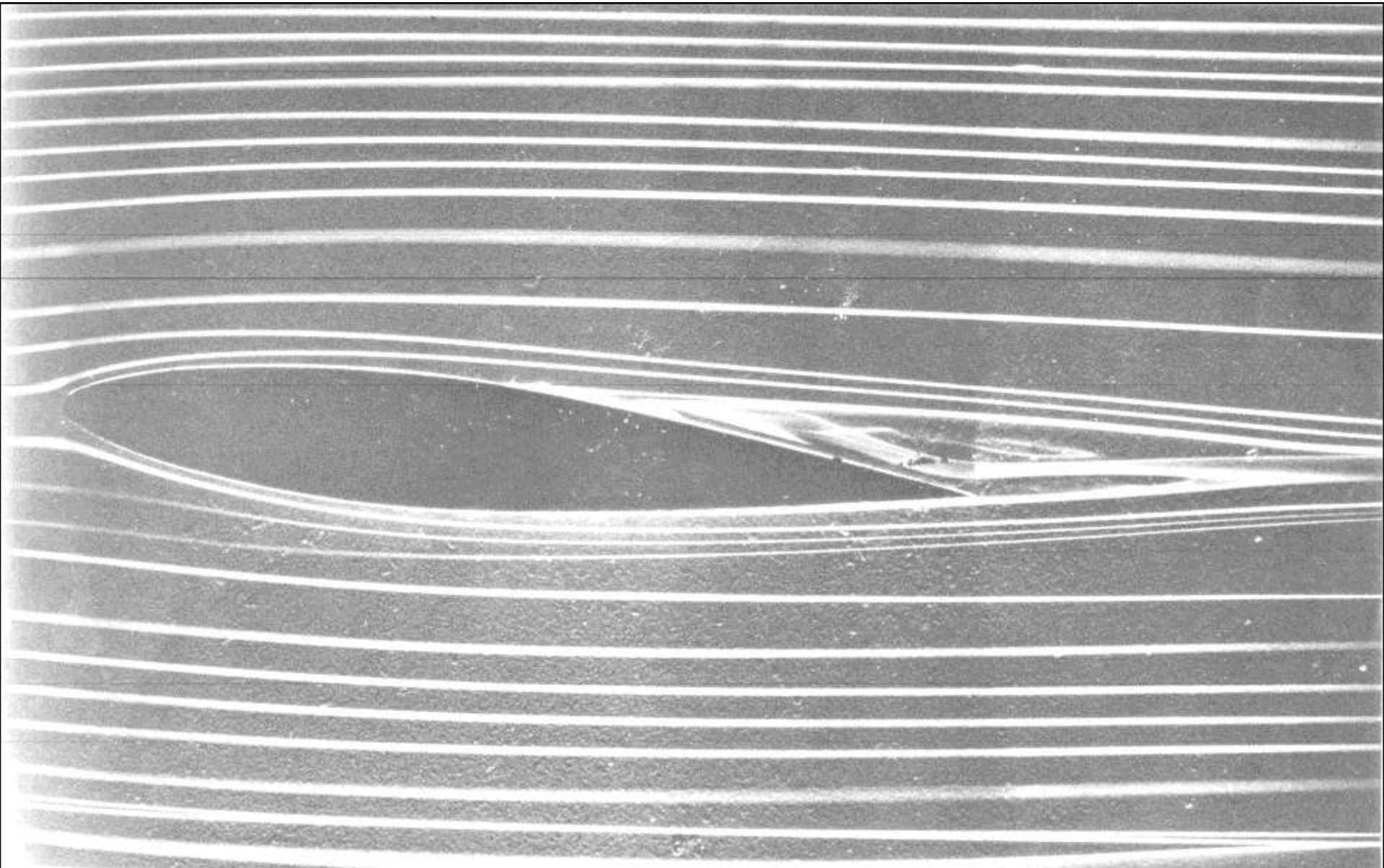
Schematic sketch of velocity profiles  $u(s, N)$  in the neighborhood of an MRS point (separation point) for steady flow over moving walls.

M: Moore, R: Rott, S: Sears



**The Goldstein Singularity**

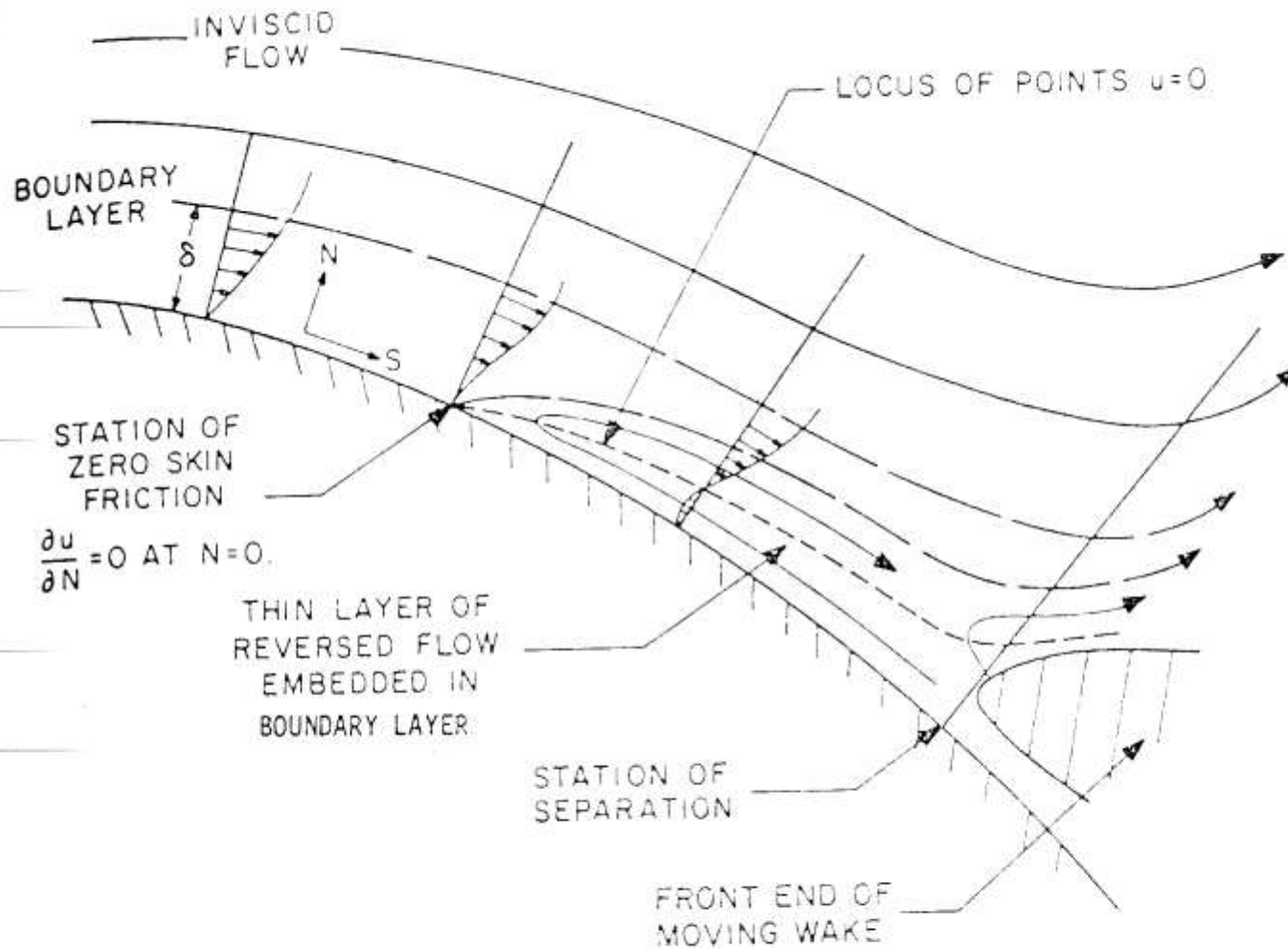
The inverse square of the v-component versus s for  $u_w / U_\infty = 0.01$ .



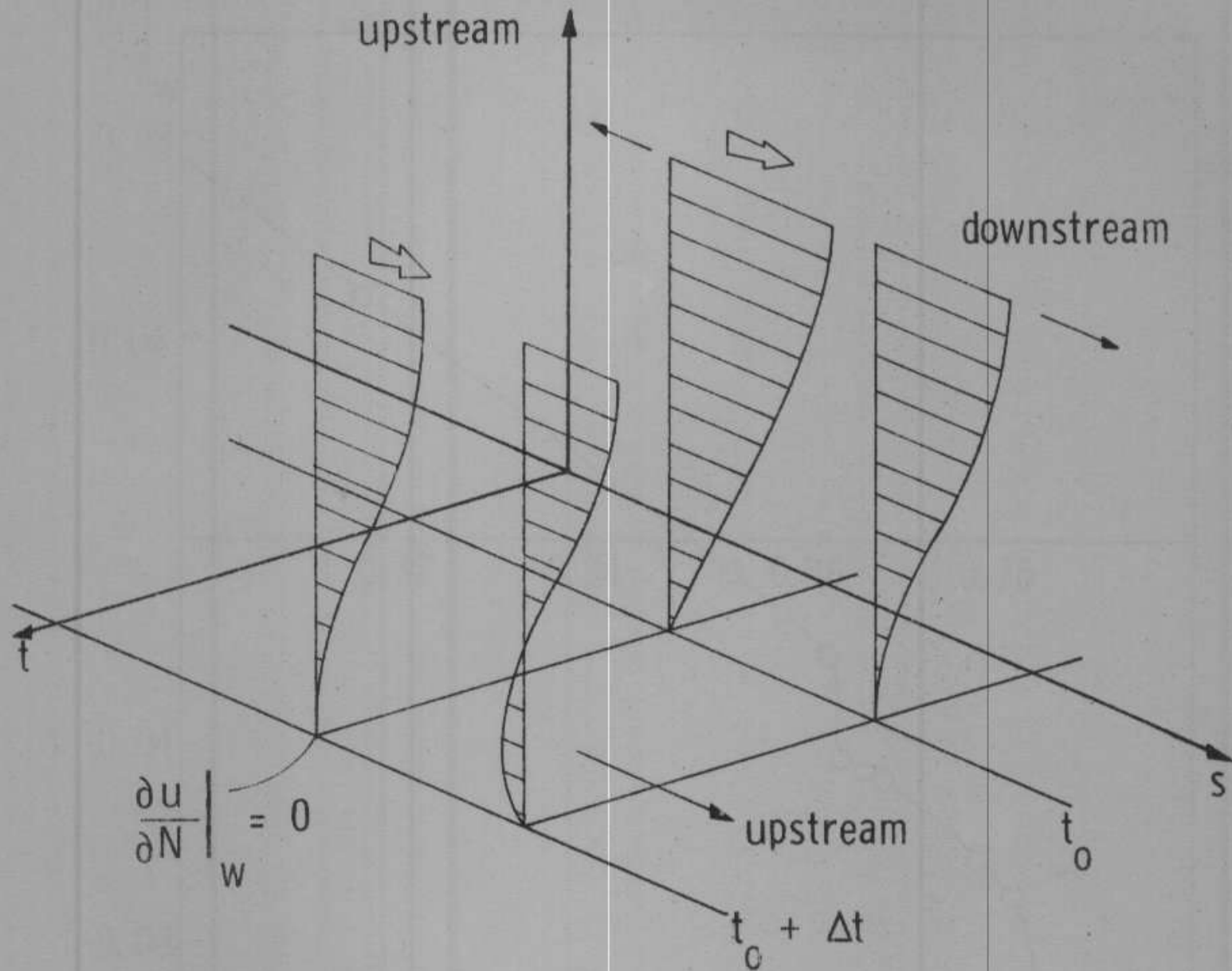
## Unsteady Boundary Layer Equations

$$\frac{\partial u}{\partial s} + \frac{\partial v}{\partial N} = 0$$

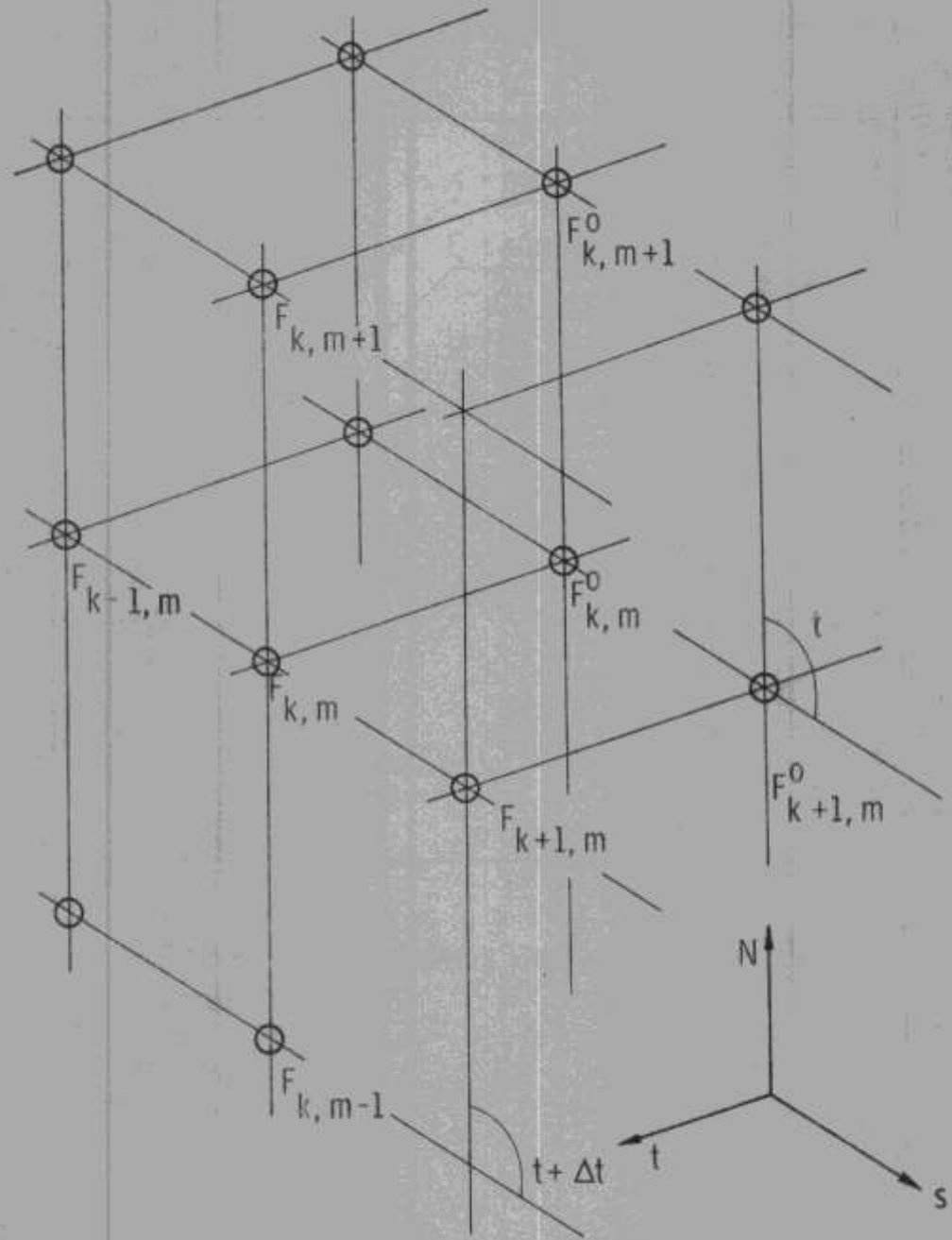
$$\frac{\partial u}{\partial t} + u \frac{\partial u}{\partial s} + v \frac{\partial u}{\partial N} - \frac{\partial U_e}{\partial t} - U_e \frac{\partial U_e}{\partial s} = \frac{\partial^2 u}{\partial N^2}$$



Schematic of the flow field in the neighborhood of unsteady separation.



Schematic sketch of the flow field



Three-dimensional mesh configuration

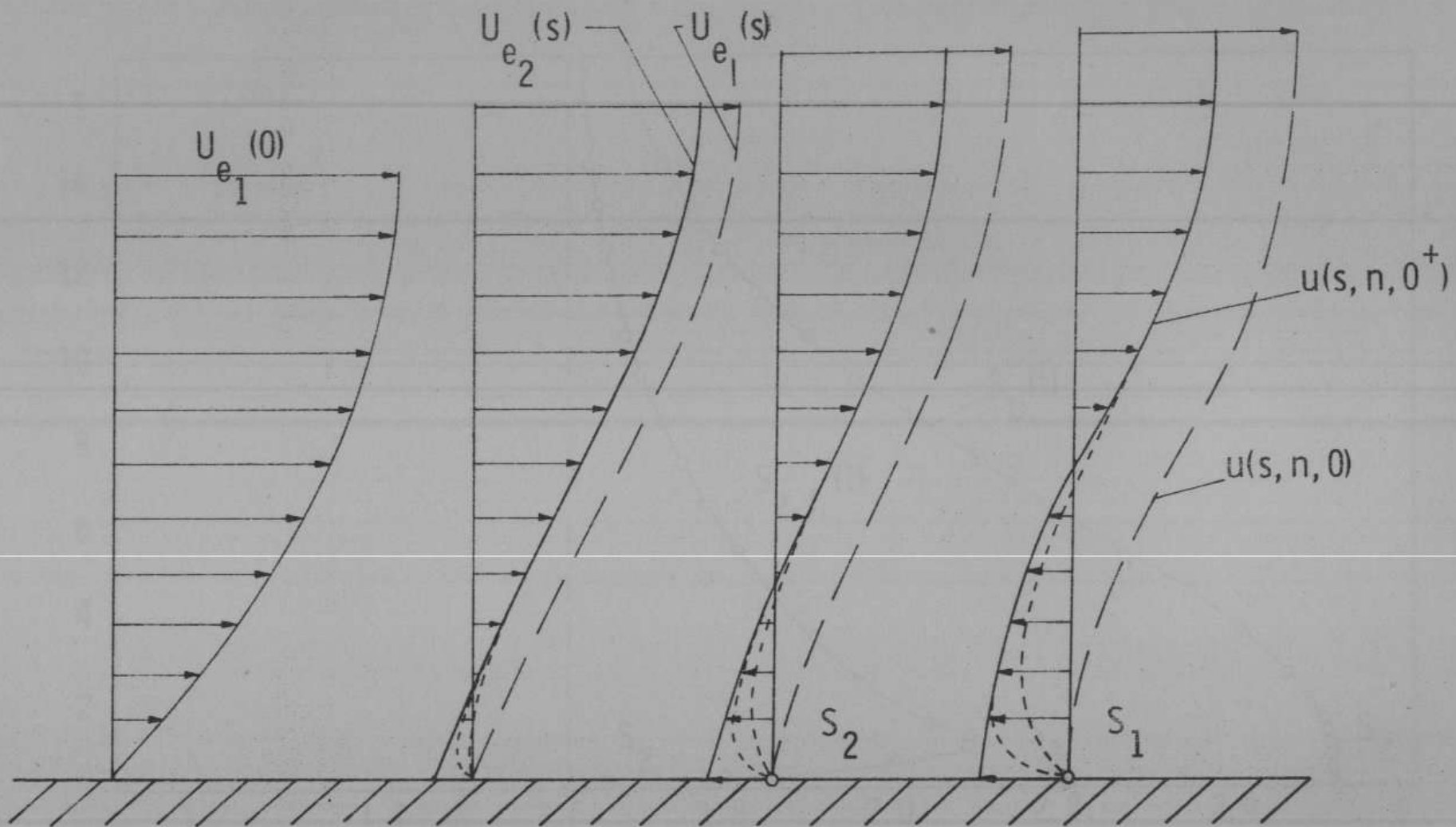
# UPWIND DIFFERENCING

The Mixed Version

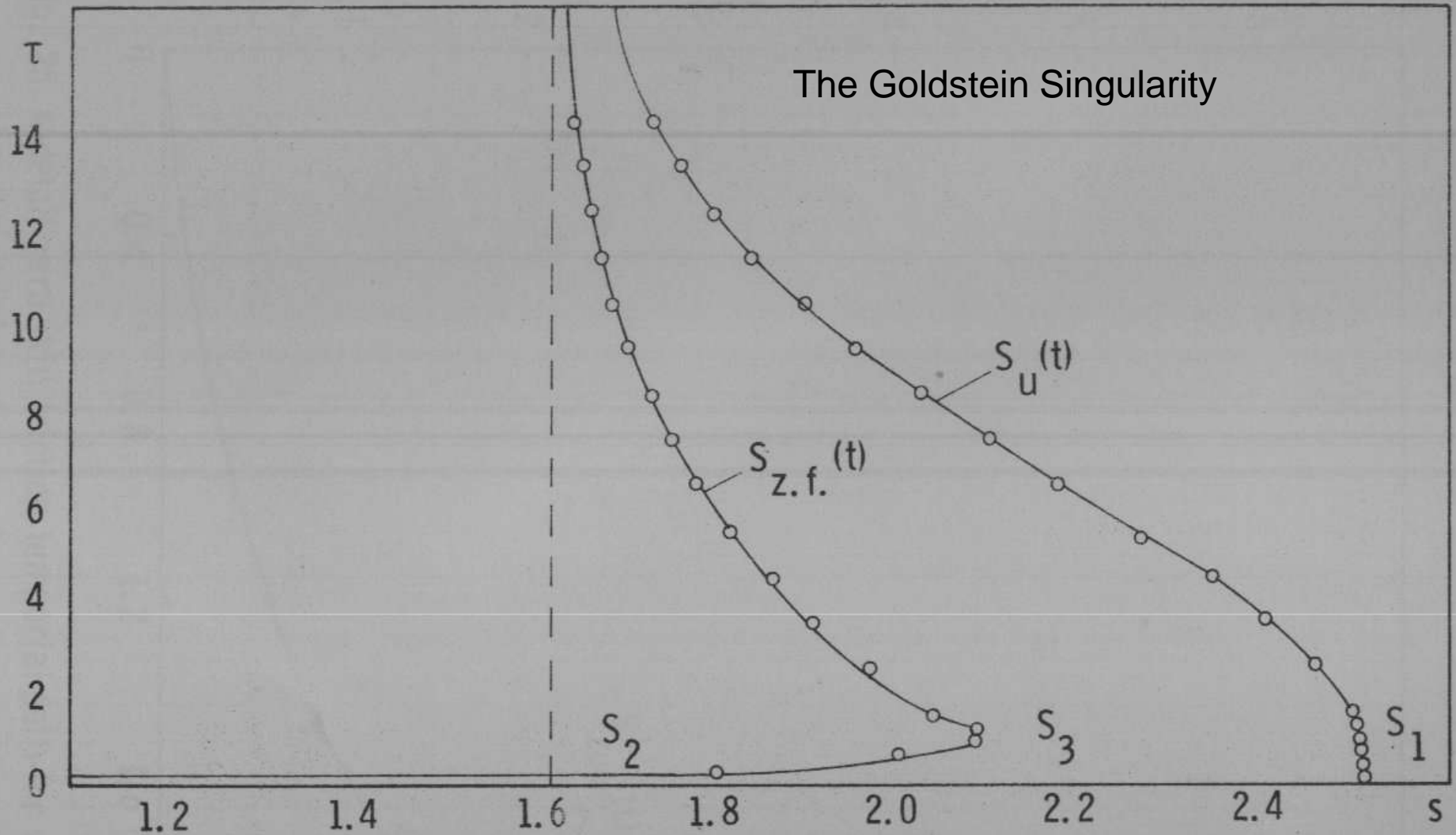
$$\left. \frac{\partial F}{\partial \xi} \right|_{k,m} \cong \frac{1}{\Delta \xi} \left( F_{k+1,m}^0 - F_{k,m} \right)$$

The Krause Version

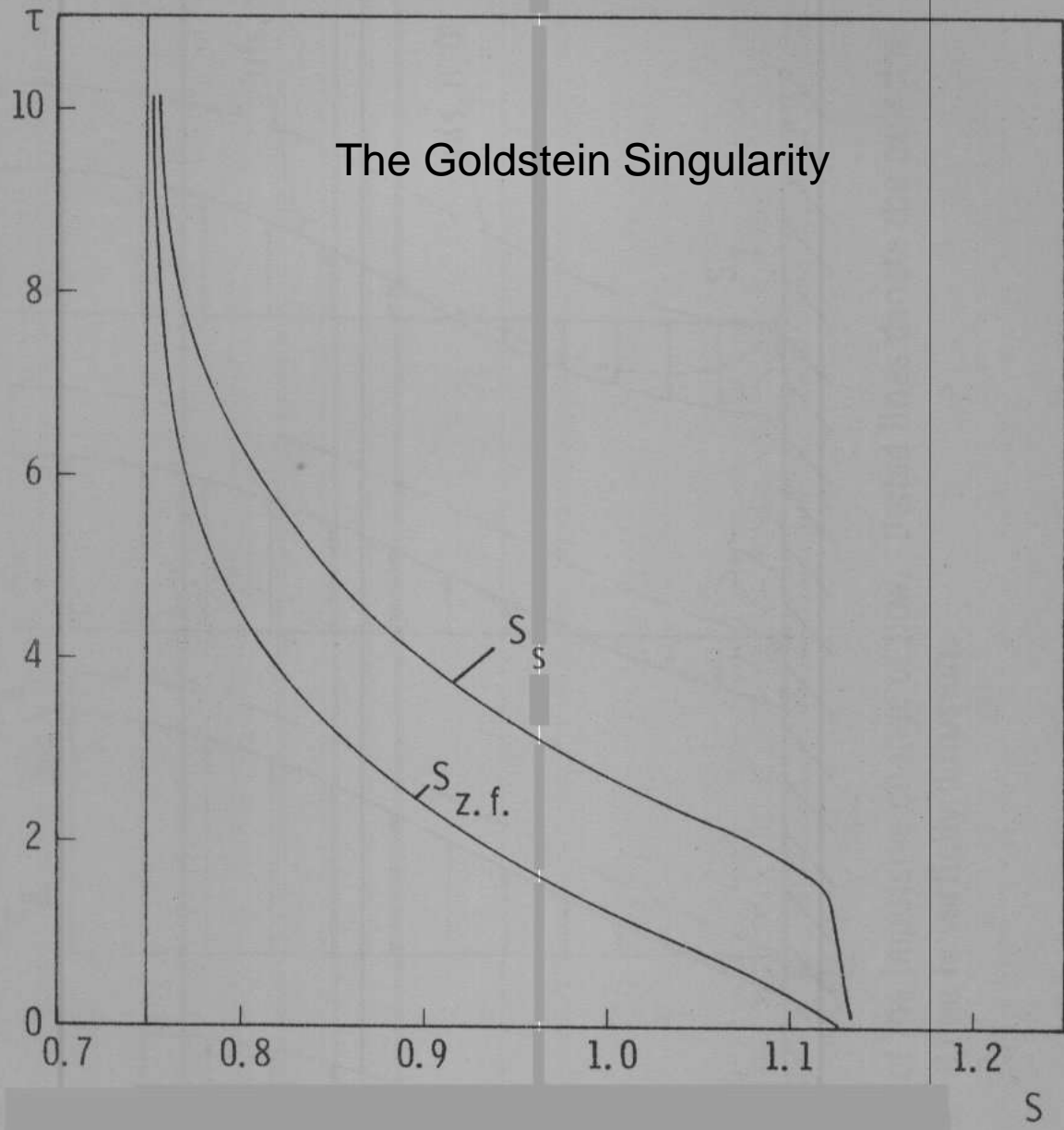
$$\left. \frac{\partial F}{\partial \xi} \right|_{k,m} \cong \frac{1}{2\Delta \xi} \left[ \left( F_{k+1,m}^0 - F_{k,m}^0 \right) + \left( F_{k,m} - F_{k-1,m} \right) \right]$$



Schematic of the impulsive change of flow. Dotted lines denote the expected change  $t = 0$  due to vorticity diffusion.



Temporial path of the points of zero skin friction and separation for an impulsive change



Temporal path of the points of zero skin friction and separation in unsteady flow